

TIME AND WORK



Worker A takes 8 hours to do a job. Worker B takes 10 hours to do the same job. How long should it take both A and B, working together but independently, to do the same job? (IGNOU, 2003)

As per the given question (5)

A takes 8 hours to do a job
 \therefore The one hour's work of A = $\frac{1}{8}$ job.

B takes 10 hours to do the same job
 \therefore The one hour's work of B = $\frac{1}{10}$ job.

As per question we found the total time of A & B 1 hour's work

$$\Rightarrow A+B = \frac{1}{8} + \frac{1}{10} = \frac{5+4}{40}$$

$$\Rightarrow \frac{9}{40} \text{ hr}$$

\therefore The total work of A & B $\left(\frac{1}{8} + \frac{1}{10} \right)$

$$\Rightarrow \frac{40 \text{ hr}}{9} = 4 \frac{4}{9} = 4 \frac{4}{9} \text{ hr}$$

A, B and C can complete a piece of work in 24, 6 and 12 days respectively. Working together, they will complete the same work in : (C.B.I. 2003)

As per the given question

A can complete a piece of work in 24 days. $\left[\frac{1}{24} + \frac{1}{6} + \frac{1}{12} \right]$
 \therefore A's one day's work = $\frac{1}{24}$ days.

B can complete a piece of work in 6 days
 \therefore B's one day's work = $\frac{1}{6}$ days

C can complete a piece of work in 12 days
 \therefore C's one day's work = $\frac{1}{12}$ days

As per the question we found the

Complete 1 work in 1 day A, B & C.

$$\rightarrow A+B+C = \frac{1}{A} + \frac{1}{B} + \frac{1}{C} = \frac{1}{24} + \frac{1}{6} + \frac{1}{12}$$

$$\Rightarrow \frac{1+4+2}{24} = \frac{7}{24}$$

\therefore The A, B, C's complete work in $\frac{24}{7}$ days
 $\Rightarrow 3\frac{3}{7}$ days

A man can do a piece of work in 5 days, but with the help of his son, he can do it in 3 days. In what time can the son do it alone? (S.S.C. 2004)

As per the given question $\frac{1}{3} - \frac{1}{5} =$

A man can do a piece of work in 5 days

\therefore The 1 day's work of man = $\frac{1}{5}$ days

As per the question with the help of his son he can complete the work within 3 days.

\therefore we found the son's work in 1 day's

$$\Rightarrow \frac{1}{3} - \frac{1}{5} = \frac{5-3}{15} = \frac{2}{15}$$

\therefore The son can complete work of his in alone $\frac{15}{2} = 7\frac{1}{2}$ days

Ronald and Elan are working on an assignment. Ronald takes 6 hours to type 32 pages on a computer, while Elan takes 5 hours to type 40 pages. How much time will they take, working together on two different computers to type an assignment of 110 pages?

As per the given question

Ronald takes 6 hours to type 32 pages

Number of pages typed in 1 hour by Ronald is = $\frac{32}{6} = \frac{16}{3}$ per

Elan takes 5 hours to type 40 pages

Number of pages typed in 1 hour by

Elan is = $\frac{40}{5} = 8$ per

Number of pages typed in 1 hour by

Number of pages typed in 1 hour by Roland and Elan = $\frac{16}{3} + 8$

$\rightarrow \frac{16+24}{3} = \frac{40}{3}$

\therefore The complete work for both is $\frac{40}{3}$

\therefore Time taken by both to type of 110 pages

$$\Rightarrow 110 \times \frac{3}{40} = \frac{33}{4} \text{ hrs} = 8 \frac{1}{4} \text{ hrs}$$

\therefore The time taken by Roland & Elan to type the 110 pages is $8 \frac{1}{4}$ hrs

P can complete a work in 12 days working 8 hours a day. Q can complete the same work in 8 days working 10 hours a day. If both P and Q work together, working 8 hours a day, in how many days can they complete the work? (Bank P.O. 1999)

As per the given question

P can complete a work in 12 days working 8 hours a day

P can complete the work in $12 \times 8 = 96$ hrs

Q can complete the same work in 8 days working 10 hours per day

Q can complete the work in $8 \times 10 = 80$ hrs

\therefore P's 1 hour work = $\frac{1}{96}$

\therefore Q's 1 hour work = $\frac{1}{80}$

\therefore (P+Q)'s 1 day work = $\frac{1}{96} + \frac{1}{80}$

$\Rightarrow \frac{11}{480}$

P+Q's complete work is $\frac{480}{11}$ days

As per question if P+Q work 8 hours per day then we found the comp work

\Rightarrow Number of days of 8 hours each.

$\Rightarrow \frac{480}{11} \times \frac{1}{8} = \frac{60}{11} \text{ days} \Rightarrow 5 \frac{5}{11} \text{ days}$

\therefore The A & B can complete the work in $5 \frac{5}{11}$ days if they work together in 8 hours per day

A is 30% more efficient than B. How much time will they, working together, take to complete a job which A alone could have done in 23 days?

As per the given question

more efficient than B. How much time will they, working together, take to complete a job which A alone could have done in 23 days?

As per the given question
A is 30% more efficient than B

∴ The ratio of A:B = $\frac{A}{B} = \frac{130}{100}$ 100
30
130%

Let B takes x days do the work

∴ A:B = $\frac{13}{10} :: 23 : x \Rightarrow \frac{13}{10} = \frac{23}{x}$

$\Rightarrow x = \frac{23 \times 10}{13}$

$\Rightarrow x = \frac{230}{13}$

∴ B takes $\frac{230}{13}$ days

∴ A's 1 day's work = $\frac{1}{23}$

B's 1 day's work = $\frac{10}{230}$

∴ We found the together work work of 1 day's work

$\Rightarrow A+B = \frac{1}{A} + \frac{1}{B} = \frac{1}{23} + \frac{10}{230} = \frac{13+10}{230}$

$\Rightarrow \frac{1}{13}$
work for 13 days

They complete the work for 13 days

A can finish a work in 18 days and B can do the same work in 15 days. B worked for 10 days and left the job. In how many days, A alone can finish the remaining work?

In the given question

A can finish a work in 18 days

∴ A's 1 day's work is $\frac{1}{18}$ day

B can do the same work in 15 days

∴ B's 1 day's work is $\frac{1}{15}$ days

∴ B's 10 days work is $\frac{1}{15} \times 10 = \frac{2}{3}$

Remain work = $1 - \frac{2}{3}$

$\Rightarrow \frac{3-2}{3} = \frac{1}{3}$

∴ The remaining work done by A
is $18 \times \frac{1}{3} = 6$

∴ The remaining work done by A in
6 days.

X and Y can do a piece of work in 20 days and 12 days respectively. X started the work alone and then after 4 days Y joined him till the completion of the work. How long did the work last? (Bank P.O. 2004)

As per the given question

X can do a piece of work in 20 days
∴ 1 day's work of X = $\frac{1}{20}$

Y can do a piece of work in 12 days.
∴ 1 day's work of Y = $\frac{1}{12}$

We find the 4 days work

$$\Rightarrow \frac{1}{20} \times 4 = \frac{1}{5}$$

Remaining work = $1 - \frac{1}{5} = \frac{5-1}{5} = \frac{4}{5}$

Now we find the 1 day's work of
A & B together

$$\Rightarrow \frac{1}{20} + \frac{1}{12} = \frac{3+5}{60} = \frac{8}{60} = \frac{2}{15}$$

They complete the work together in $\frac{15}{2}$ days

So $\frac{4}{5}$ of work done by X & Y

$$\Rightarrow \frac{15}{2} \times \frac{4}{5} = 6$$

∴ Hence the total time taken by A & B

$$\Rightarrow 6 + 4 = 10 \text{ days}$$

A, B and C together earn Rs. 300 per day, while A and C together earn Rs. 188 and B and C together earn Rs. 152. The daily earning of C is

As per the given question

A, B & C together earn Rs. 300 per day

A & C together earn Rs. 188

B & C together earn Rs. 152

A & C together earn Rs 188
 B & C together earn Rs 152

\therefore A's daily income is $300 - 152 = 148$
 \therefore B's daily income is $300 - 188 = 112$

$(A+B+C) - (A+B)$

Now we found the C's daily income

$(A+B+C) - (A+B)$

$$\rightarrow 300 - (148 + 112)$$

$$= 300 - 260$$

$$\rightarrow 40$$

\therefore the daily salary of C is Rs. 40

If 6 men and 8 boys can do a piece of work in 10 days while 26 men and 48 boys can do the same in 2 days, the time taken by 15 men and 20 boys in doing the same type of work will be:

- (a) 4 days (b) 5 days

(S.S.C. 1999)

As per the given question

6 men & 8 boys can do a piece of work = 10 days

Let the 1 man's 1 day's work is x

1 boy's 1 day's work is y

$$\rightarrow 6x + 8y = \frac{1}{10}$$

1 day's work of 26 men & 48 boys

$$\rightarrow 26x + 48y = \frac{1}{2} \quad \text{--- (ii)}$$

Solving the eqn (i) & (ii)

$$\rightarrow 6x + 8y = \frac{1}{10}$$

$$\rightarrow 26x + 48y = \frac{1}{2}$$

$$\therefore x = \frac{1}{100}, y = \frac{1}{200}$$

\therefore we found the 1 day's work of 15 men & 20 boys

∴ we found the ¹⁰⁰ days work of 15m & 20 boys

$$\Rightarrow 15 \times \frac{1}{100} + 20 \times \frac{1}{200} \Rightarrow \frac{15}{100} + \frac{20}{200}$$

$\rightarrow \frac{1}{4} \Rightarrow 4$

∴ ~~The~~ 20 boys complete work of 15m in 4 days.